

# L<sup>A</sup>T<sub>E</sub>X equations for VStar

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## 1 Standard error of the average

$$StdErr = \frac{\sqrt{\frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N-1}}}{\sqrt{N}}$$

## 2 Phase

$$\phi = \frac{t - epoch}{P}$$

## 3 WWZ

### 3.1 Time Steps

$$quantize(x) = \begin{cases} 5 \times 10^{\lfloor \log_{10} x \rfloor}, & \text{if } \frac{x}{10^{\lfloor \log_{10} x \rfloor}} \geq 5 \\ 2 \times 10^{\lfloor \log_{10} x \rfloor}, & \text{if } \frac{x}{10^{\lfloor \log_{10} x \rfloor}} \geq 2 \\ 1 \times 10^{\lfloor \log_{10} x \rfloor}, & \text{if } \frac{x}{10^{\lfloor \log_{10} x \rfloor}} < 2 \end{cases}$$

$$t_{span} = t_n - t_1$$

$$t_{step} = quantize\left(\frac{t_{span}}{t_{div}}\right)$$

$$tau_1 = t_{step} \times \frac{t_1}{t_{step} + 0.5}$$

$$tau_n = t_{step} \times \frac{t_n}{t_{step} + 0.5}$$

$$tau = [tau_1, tau_1 + t_{step}, tau_1 + 2t_{step}, tau_1 + 3t_{step}, \dots, tau_n]$$

where  $\lfloor \log_{10} x \rfloor$  is the integer part of  $\log_{10} x$ ,  $t_n$  is the maximum time value (e.g. maximum JD) in the dataset,  $t_1$  is the minimum time value,  $t_{div}$  is the number of time divisions specified by the user,  $t_{step}$  is the resulting time step, and  $tau$  is the set of time values upon which the time-frequency analysis is based. One set of WWZ statistics is computed per frequency per  $tau$  value.

## 4 Polynomial fit

### 4.1 Equation

$$y = f(t) = \beta_0 + \beta_1 t + \beta_2 t^2 + \beta_3 t^3 + \dots + \beta_n t^n$$

### 4.2 Root Mean Square (RMS)

$$RMS = \sqrt{\frac{\sum_{i=1}^n (y - \hat{y})^2}{n}}$$

where  $n$  is the number of observations,  $y$  is the observed magnitude, and  $\hat{y}$  is the model predicted magnitude (with  $y - \hat{y}$  giving the residual value).

### 4.3 Akaike Information Criteria (AIC)

$$AIC = \frac{\sum_{i=1}^n (y - \hat{y})^2}{n} + 2deg$$

where  $N$  is the number of observations,  $y$  is the observed magnitude and  $\hat{y}$  is the model predicted magnitude (with  $y - \hat{y}$  giving the residual value), and  $deg$  is the polynomial's degree (e.g. 2 if the highest order term is  $\beta_2 t^2$ ).

### 4.4 Bayesian Information Criteria (BIC)

$$BIC = \frac{\sum_{i=1}^n (y - \hat{y})^2}{n} + deg \ln(n)$$

where  $n$  is the number of observations,  $y$  is the observed magnitude,  $\hat{y}$  is the model predicted magnitude (with  $y - \hat{y}$  giving the residual value), and  $deg$  is the polynomial's degree (e.g. 2 if the highest order term is  $\beta_2 t^2$ ).

## 5 DCDFT

### 5.1 standard scan

$$\frac{1}{\text{frequency}}$$
$$\frac{1}{4T}$$
$$\frac{N}{4T}$$

### 5.2 period error

#### 5.2.1 standard error of the frequency

$$s_v = \sqrt{\frac{6s^2}{\pi^2 N A^2 T^2}}$$

where  $s^2$  is the sample variance of the residuals:

$$s^2 = \frac{\sum (X - \bar{X})^2}{N - 1}$$

$N$  is the number of data points,  $A$  is the semi-amplitude of the sinusoid for the period in question, and  $T$  is the total time span of the data.

#### 5.2.2 standard error of the semi-amplitude

$$s_A = \sqrt{\frac{2s^2}{N}}$$

where  $A$  is the semi-amplitude of the sinusoid for the period in question,  $s^2$  is the sample variance of the residuals,  $N$  is the number of data points.